# An Evolutionary Autonomous Agents Approach to Image Feature Extraction

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Abstract— This paper presents a new approach to image feature extraction which utilizes evolutionary autonomous agents. Image features are often mathematically defined in terms of the gray-level intensity at image pixels. The optimality of image feature extraction is to find all the feature pixels from the image. In the proposed approach, the autonomous agents, being distributed computational entities, operate directly in the two-dimensional lattice of a digital image, and exhibit a number of reactive behaviors. In order to effectively locate the feature pixels, individual agents sense the local stimuli from their image environment by means of evaluating the gray-level intensity of locally connected pixels, and accordingly activate their behaviors. The behavioral repository of the agents consists of: (1) featuremarking at local pixels and self-reproduction of offspring agents in the neighboring regions if the local stimuli are found to satisfy feature conditions, (2) diffusion to adjacent image regions if the feature conditions are not held, or (3) death if the agents exceed their life span. As part of the behavior evolution, the directions in which the agents self-reproduce and/or diffuse are inherited from the directions of their selected high-fitness parents. Here the fitness of a parent agent is defined according to the steps that the agent takes to locate an image feature pixel.

Keyword— Evolutionary computation, autonomous agents, self-reproduction, diffusion, image feature extraction.

# 1 Introduction

In computer vision and image processing, image features like edges, lines, curves, corners, and borders may be detected using some mathematically defined operators, such as gradient edge detectors and zero-crossing edge detectors, or using surface fitting methods [12]. Detecting these features can greatly facilitate the interpretation of the scenes.

Many sophisticated techniques and algorithms for image feature extraction have been proposed and applied in recent years [4, 5, 21, 23, 26]. For instance, Liow [21] proposed an extended border tracing technique that combines the operations of region finding and closed contour detection. Alter and Basri [1] applied the so-called Salient Network method for extracting salient curves and noted that this method could suffer the problem of failing to identify any salient curve other than the most salient one (according to their proposed saliency measure). Lee and Kim [20] presented a method of extracting topographic features directly from a gray-level character image, without calculating eigenvalues and eigenvectors of the

underlying image intensity surface. The method efficiently computes the directions of principal curvature. Maintz et al. [25] investigated the problem of evaluating ridge seeking operators for multimodality medical image matching.

With conventional approaches to image feature extraction, all the possible feature patterns must be carefully enumerated and exhaustively searched. This represents a non-trivial task. Furthermore, the resulting template masks may be sensitive to noise in the image. Another disadvantage is that the complexity of image feature extraction (e.g., a closed border for a region) is determined by the complexity of the images. For instance, in a spiral-like environment, the template-based border tracing method [21] can be slowed down simply due to the length of the border to be traversed.

The approach introduced here utilizes evolutionary autonomous agents that can self-reproduce, diffuse, and cease to exist during the course of interacting with a digital image environment. The most distinct characteristics of our approach lie in that it is bottom-up, decentralized, and distributed in nature, and relies on local agent "processes" whose behaviors are both easy to define and natural for software and hardware implementations. This paper demonstrates such an agent system through illustrative examples in which a class of agents is equipped with the above mentioned behaviors in order to extract features from the image.

#### 1.1 Related Work

Evolutionary computation is concerned with applying the computational models of evolutionary processes (e.g., [3]) to either achieving intelligent agent behaviors, where intelligence is measured in terms of the agent ability to contribute to its self-maintenance at genetic, structural, individual, as well as group levels [34], or solving real-life computation-intensive engineering problems, such as numerical optimization. In recent years, researchers in this field have been studying and advancing the methodologies for evolutionary computation as well as their applications in a number of areas, including genetic algorithms, evolution strategies, genetic programming, evolutionary programming, and classifier systems [10, 11, 13, 15, 16, 28, 29, 32]. Fogel [9] has provided a thorough treatment on the foundation and scope of this field.

Evolutionary autonomous agent systems as applied to digital image processing is a newly-explored area of research that studies the emergent behaviors in a lattice where agents react to the digital image environment according to a set of behavioral rules. It may be viewed as a further extension to the earlier work on cellular automata [8, 17, 18, 19, 22, 24]. Cellular automata, which drew upon Von Neumann's model [31], is concerned primarily with the fixed-point properties in a lattice of finite automata in which cells act locally according to a set of cellular rules [22]. Shanahan [33] investigated a class of cellular automata in which a population of organisms evolves in a microworld of square grid locations by repeatedly executing four local procedures, namely, cease to exist, move, merge, and duplicate. The goal of his work was to experimentally investigate under what conditions an instance of cellular automata could produce a significant amount of complexity and diversity. Tamayo and Hartman [35] applied computational organisms to model reaction-diffusion systems from which interesting space-time patterns reminiscent of chemical turbulence, solitons, and self-excited oscillations could be constructed and observed.

The proposed autonomous agent model exhibits general cellular behavior characteristics similar to those of cellular automata, but with the following fundamental differences; namely: (1) in the proposed agent model, the automata operate in a gray-level digital image and hence inanimate stimuli are present in the cellular environment, and (2) the behaviors of agents evolve as a result of the interaction with and within the image environment, whereas in cellular automata they are manually pre-defined.

#### 1.2 Organization of the Paper

The remainder of this paper is organized as follows: Section 2 formally states the global optimality criterion of image feature extraction from the point of view of the evolutionary autonomous agents approach. Section 3 gives the representation of the proposed autonomous agents, their reactive behaviors, and the algorithm underlying the agent-based image feature extraction. Section 4 describes several experiments in which the agent-based approach is effectively applied to extract image edges and multiple features, and to follow dynamically moving features. Section 5 discusses the dynamics of the agent population, and examines the issues such as the effects of behavioral parameters on the computation. Finally, Section 6 concludes the paper by highlighting the key contributions of this work.

# 2 Problem Statement

The two-dimensional lattice in which the proposed autonomous agents reside is a gray-level image,  $\mathcal{I}$ , of size  $U \times V$  (i.e., an array of U rows by V columns of pixels). Suppose that  $\mathcal{I}$  contains a number of pixels whose intensity relative to those of its neighboring pixels satisfies certain mathematically well-defined conditions. These pixels are called feature pixels. The objective of the autonomous agents in  $\mathcal{I}$  is to extract all the pre-defined features of  $\mathcal{I}$  by finding and marking at the feature pixels. This is essentially an optimization problem as stated below.

**Definition 2.1 (Optimal feature extraction)** Let M denote the total number of feature pixels in  $\mathcal{I}$ . If the total number of feature pixels detected and marked by active agents is equal to M, it is said an optimal feature extraction is achieved.

**Definition 2.2 (Active agents)** At a certain time t in the two-dimensional lattice, autonomous agents whose age does not exceed their life span will continue to react to their image environment by way of evaluating the pixel gray-level intensity and selecting accordingly some of their behaviors. Such agents are called the active agents at time t.

From the above notions, we can further define an efficiency measure of the optimal feature extraction during a given period of discrete time, t, as the average rate of success that active agents find image features during t. Here, the rate of success is defined as the ratio between the total number of extracted feature pixels over the total number of active agents being used during t.

**Definition 2.3 (Efficiency of optimal feature extraction)** The efficiency measure of an optimal feature extraction by autonomous agents for t time intervals is defined as the following function:

$$Q(t) = \frac{1}{t} \sum_{\tau=1}^{t} \left( \frac{\sum_{k=0}^{\tau} m(k)}{\sum_{k=0}^{\tau} N_{\Phi}(k)} \right)$$
 (1)

where

m(k): the number of extracted feature pixels found at time k, and  $N_{\Phi}(k)$ : the number of active autonomous agents  $\Phi$  in  $\mathcal I$  at time k.

From Definition 2.3, it is clear that the higher the Q(t) value, the higher efficiency of feature extraction will become.

# 3 Evolutionary Autonomous Agents for Image Feature Extraction

The evolutionary nature of the proposed agents approach lies in the way in which the generations of autonomous agents are selected and replicated. This section presents the detailed definitions of evolutionary autonomous agents, including their environment properties, local pixel evaluation function, fitness function, and the evolution of diffusion and asexual self-reproduction behaviors.

# 3.1 Two-dimensional Lattice of an Agent Environment

Autonomous agents operate in a rectangular lattice that corresponds to a digitized image. In the rectangular lattice, each eight-connected grid represents an image pixel, as illustrated in Figure 1. The grid also signifies a possible location for an autonomous agent to inhabit, either temporarily or permanently.

**Definition 3.1** (Neighboring region of an agent) The neighboring region of an agent at pixel p is a circular region centered at pixel p with radius  $\kappa$ . The pixels falling inside this region are called the neighboring pixels of the agent. Each of the neighboring pixels is located in one of the eight evenly divided sectors. These sectors are also referred to as the eight directions of the region. Figure 1 shows an example of the neighboring pixels of an agent from eight directions, respectively, when  $\kappa = 1$ .

## 3.2 Local Stimulus in Two-dimensional Lattice

An autonomous agent is coded such that it always checks its neighboring region, and selects its behavior according to the concentration of certain gray-level pixels. If the concentration is within a specific range, the agent will activate its self-reproduction mechanism. Such a concentration is considered as a triggering local stimulus to the agent.

**Definition 3.2 (Local stimulus)** The local stimulus that selects and triggers the behaviors of an agent at pixel location (i, j) is computed from the sum of the pixels belonging to a neighboring region which satisfy the following condition: the difference between their gray-level intensity values and the value at (i, j) is less than a positive threshold. In other words, the stimulus is determined by the density distribution of all the pixels in its neighboring region whose gray-level intensity values are close to the intensity at (i, j), as illustrated in Figure 2. More specifically, the density distribution is defined as follows:

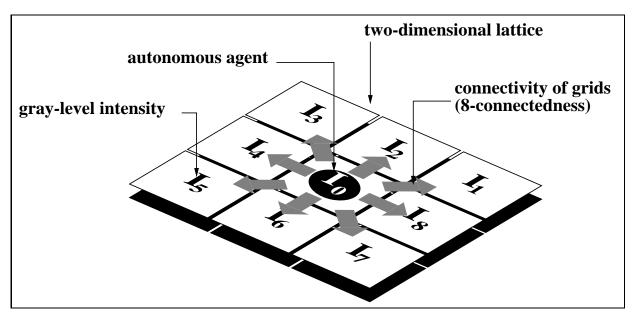


Figure 1: Each pixel in the two-dimensional lattice environment is connected to eight neighbors (i.e., eight-connectedness). An autonomous agent can check, self-reproduce, and diffuse to any one of these neighboring locations.

$$D_{I(i,j)}^{\kappa} = \sum_{s=-\kappa}^{\kappa} \sum_{t=-\kappa}^{\kappa} \{1 \mid || I(i+s,j+t) - I(i,j) || < \delta \}$$
 (2)

where

 $\kappa$ : the radius of agent neighboring region, i.e., a circular region centered at (i,j),

i, t: the indices of a pixel belonging to the neighboring region relative to (i, j),

I(i, j): the gray-level value at (i, j), and

 $\delta$ : a pre-defined positive threshold.

#### 3.3 Agent Behaviors

During the course of evolution, each of the agents in the lattice will exhibit several behaviors, e.g., self-reproducing, randomized/non-randomized search. These behaviors are triggered by the external stimuli present in the environment, which are computed using Eq. 2. As a result of the agent behavior execution, certain patterns, i.e., markers left behind by the agents, will emerge, which in turn characterize the features in the digital image environment. This section provides a detailed description of the reactive behaviors of an autonomous agent.

## 3.3.1 Feature Marking

When an agent detects a feature pixel, p, it will place a fixed marker at p. There may be different kinds of features in an image, hence several kinds of markers may exist. The stimulus for selecting the feature-marking behavior can be defined as follows:

**Definition 3.3 (Feature-marking)** Let  $\lambda = [u, v]$  be an acceptable range of the pixel count as defined using Eq. 2, where  $u \leq v$ . The agent places a marker at pixel p, if the outcome of its evaluation of the density distribution at p falls inside the  $\lambda$  interval, i.e.,  $D_{I(i,j)}^{\kappa} \in \lambda$ .

Figure 2 presents an example in which circles placed within individual grids denote the markers.

## 3.3.2 Agent Fitness Function

Two of the most important behaviors of an agent are diffusion and self-reproduction. Both can be executed in either a directional or a non-directional mode. In the directional mode, the agent selects the most effective parent agents among all the previously successful ones, and copies the directions as used in their reproduction and diffusion. The selection of the parent agents is based on their fitness function values. What follows defines the agent fitness function:

Definition 3.4 (Agent fitness function) Let  $F(\phi_i)$  denote the fitness value of an agent  $\phi_i$ . Thus,  $F(\phi_i) = \begin{cases} 1 - \frac{N \text{ steps before self-reproduction}}{\text{life\_span of } \phi_i} & \text{if } \phi_i \text{ finds triggering stimulus,} \\ -1 & \text{otherwise.} \end{cases}$ (3)

As can be noted from the above definition, the fitness function measures how long it takes the agent to find a feature pixel. The maximum fitness value is equal to one if the agent is exactly placed at the feature pixel at the time of being reproduced.

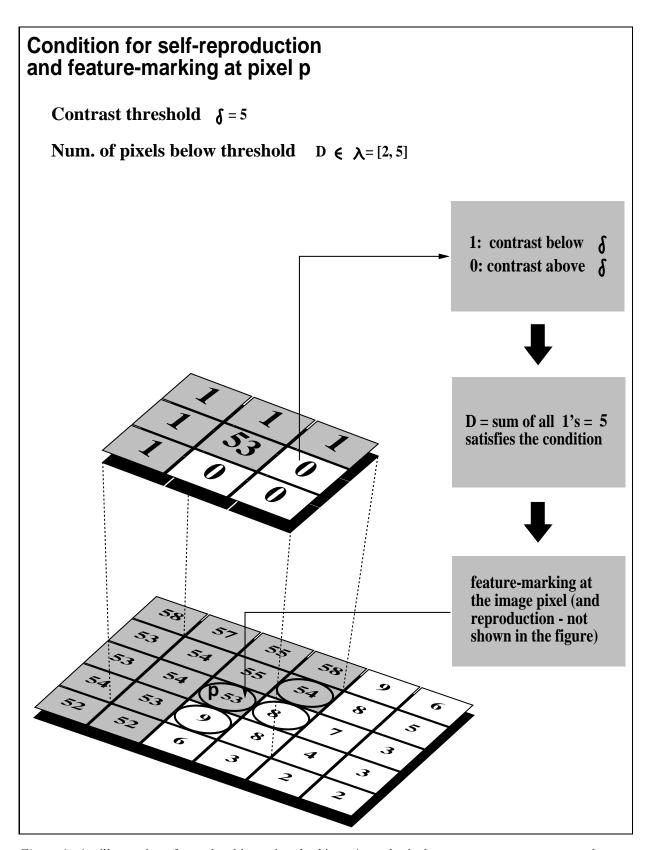


Figure 2: An illustration of gray-level intensity checking. At each pixel p, an autonomous agent evaluates the outcomes of applying a mathematically well-defined operator. If the specific feature condition is satisfied, the agent leaves a permanent feature-marker at the pixel location.

#### 3.3.3 Diffusion

According to Definition 2.2, an active agent always evaluates the pixel gray-level intensity of a neighboring region relative to its current location in order to see whether or not this location can be regarded as a feature pixel, i.e., a pixel that satisfies the condition as stated in Definition 3.3. If the current location is not a feature pixel, the agent will exhibit a diffusion behavior by moving to a new location within its neighboring region in either a directional or a non-directional (i.e., random-direction) mode. The length of diffusion will be randomly generated. The diffusion behavior plays an important role for the agent to search feature pixels within the two-dimensional lattice. The specific stimulus that triggers this behavior is given as follows:

**Definition 3.5 (Directional diffusion)** Let  $\lambda = [u, v]$  be an acceptable range of the pixel count as defined using Eq. 2, where  $u \leq v$ . The agent moves to its adjacent locations whenever the outcome of its evaluation of the density distribution falls outside the  $\lambda$  interval, i.e.,  $D_{I(i,j)}^{\kappa} \notin \lambda$ . The direction of the diffusion is selected based on an eight-element probability vector (corresponding to eight evenly divided directional sectors) in which each value indicates the probability of becoming high-fitness if the agent diffuses in the corresponding direction. The length of the diffusion is randomly generated within the diffusion region.

The direction vector of the agent as mentioned in the above definition is updated based on the diffusion directions of its previously selected high-fitness parent agents, as illustrated in Figure 3. The details on the updating computation are given in Section 3.3.5.

#### 3.3.4 Self-reproduction

If an agent detects a feature pixel, p, it will reproduce a finite number of offspring agents within its neighboring region in either a directional or a non-directional (i.e., random-direction) mode. The self-reproduction behavior enables the agent to distribute offspring agents near the pixel location that meets the feature definition, and hence increases the likelihood of further feature extraction.

**Definition 3.6 (Directional self-reproduction)** Let  $\lambda = [u, v]$  be an acceptable range of the pixel count as defined using Eq. 2, where  $u \leq v$ . The agent self-reproduces a finite number of offspring agents within its neighboring region of radius  $\kappa$  in a direction as computed from its direction probability vector, if the outcome of its evaluation of the density distribution at p falls inside the  $\lambda$  interval, i.e.,  $D_{I(i,j)}^{\kappa} \in \lambda$ . The distance of the offspring from the parent agent inside the self-reproduction region will be randomly generated.

Figure 4 illustrates the self-reproduction behavior of an autonomous agent. The direction vectors of self-reproduction by the agent (and subsequently by its offspring) depend on an updating mechanism as given in Section 3.3.5.

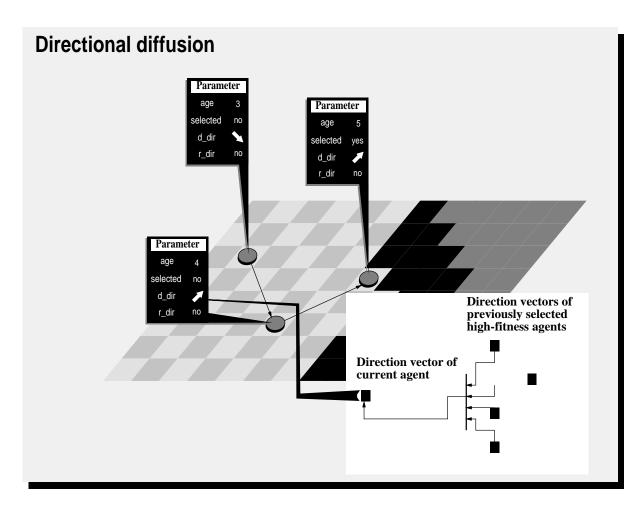


Figure 3: An illustration of agent diffusion behavior. An autonomous agent of age 3 diffuses to its neighboring region of the two-dimensional lattice, in a direction as updated based on the directions of the previously selected agents (see Section 3.3.5). After each diffusion step, the age of the agent will be incremented by one. The process of diffusion provides a chance for the agent to search image features from the locations of its parent agents.

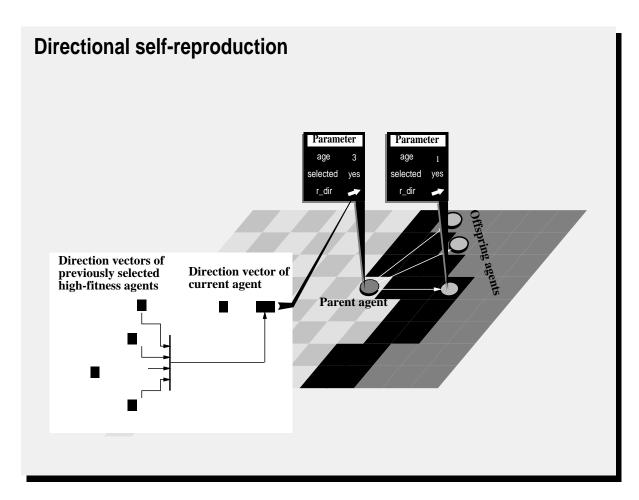


Figure 4: An illustration of agent self-reproduction behavior. The asexual self-reproduction of an agent is triggered by the external stimuli in the environment as computed from the density distribution of their neighboring pixels of certain gray-level intensity values. The process of diffusion and self-reproduction repeats during the evolution of the autonomous agent population. The direction of self-reproduction is determined by a direction vector as computed from those of previously selected high-fitness parent agents.

#### 3.3.5 Direction Vector Updating

Assume that a grandparent agent  $\phi_i^{(g-1)}$  of generation g-1 produces a set of parent agents  $\{\phi_{ij}^{(g)}\}$ . This set further produces the offspring of generation g+1, as denoted by  $\{\phi_{ijk}^{(g+1)}\}$ . Thus, the directions of diffusion and self-reproduction by agent  $\phi_{ijk}^{(g+1)}$  will be updated using the directions of some selected agents from  $\{\phi_{ij}^{(g)}\}$  and  $\{\phi_{ijk}^{(g+1)}\}$ . The selection of these agents is based on their fitness values as computed using Eq. 3.

What follows provides the details on the updating mechanism for an autonomous agent to compute its diffusion and self-reproduction direction vectors. Here, a direction vector specifies the probability of success in locating image features if the corresponding direction is chosen for the respective behavior.

More specifically, the probabilities as associated with directions  $\theta$  and  $\omega$ , respectively, for diffusion and self-reproduction by agent  $\phi_{ijk}^{(g+1)}$  are derived in the following two steps:

Step 1. Agent selection: Select all  $\phi \in \{\phi_{ij}^{(g)}\}$  and  $\{\phi_{ijk}^{(g+1)}\}$ , s.t.  $F(\phi) > 0$ ; and

Step 2. Direction vector updating: For all the selected agents, compute:

$$p(\theta \in \Theta)_{\phi} = \frac{N_{\theta}}{\sum_{\forall i} N_{i}} \tag{4}$$

and

$$p(\omega \in \Omega)_{\phi} = \frac{O_{\omega}}{\sum_{\forall i} O_{i}} \tag{5}$$

where

 $\Theta$ : the set of possible directions for agent diffusion,

 $\Omega$ : the set of possible directions for agent self-reproduction,

 $N_i$ : the number of agents that have diffused to the local stimulus from direction i, and

 $O_i$ : the number of agents reproduced by their parents from direction i.

The above formulas generate the probability distributions for the diffusion and self-reproduction directions by way of calculating the percentage of occurrences.

#### 3.3.6 Agent Vanishing ("Death")

When the age of an agent exceeds its life span, the agent will abort further feature-searching movements and vanish from the two-dimensional lattice environment.

As can readily be noted from the above overview, the reactive behaviors of autonomous agents are parameterized by a set of attributes as summarized in Table 1.

#### 3.4 An Example

Taking border-tracing agents as an example, when an agent of border-sensitive class reaches a border location, it will *permanently* reside at the border and proceed to self-reproduce some offspring within its immediate neighboring region, as shown in Figure 4. This process is best illustrated in the following

Attribute	Description	Value
c	class identifier	char label
δ	intensity contrast threshold	> 0
λ	acceptable range of density value	$[u, v], \ v \ge u > 0$
s	number of offspring self-reproducible	> 0
$\Delta$	life span	$(0, \mathtt{life\_span}]$
$P(\Theta)$	direction vector for diffusion	$\Theta = \{1, 2, \cdots, 8\}$
$P(\Omega)$	direction vector for self-reproduction	$\Omega = \{1, 2, \cdots, 8\}$
$\kappa$	radius of diffusion and self-reproduction region	(1, K]

Table 1: The attributes that determine agent behaviors

reaction scheme:

$$\Phi_{i \in \{i \cap border \neq \emptyset\}}^{(g)} \xrightarrow{\text{behavioral selection}} \Phi_{j \in \{\|i-j\| \leq \kappa\}}^{(g+1)} \oplus \tilde{\Phi_i}^{(g+1)}$$

$$\tag{6}$$

where  $\Phi_i^{(g)}$ ,  $\Phi_j^{(g+1)}$ , and  $\tilde{\Phi_i}^{(g+1)}$  denote the agents reaching the border, the reproduced agents within the adjacent neighboring locations, and the agents immobilized at border i (i.e., feature-markers), respectively.  $\oplus$  symbolizes that the results are generated from two concurrently selected behaviors.

As the reproduced agents move away from the their current locations, some of them will encounter other parts of the border again, and hence the self-reproduction cycle will repeat itself, while those whose age exceeds their life span will vanish.

## 3.5 The Agent Computation Algorithm

The complete algorithm for agent-based image feature extraction is given in Figure 5.

# 4 Experiments on Image Feature Extraction

The preceding section has provided a formal model of autonomous agent behaviors. This section further examines how such agents can be applied in digital image environments in order to extract some interesting image features. In particular, we present some typical image processing experiments on edge/border detection and following.

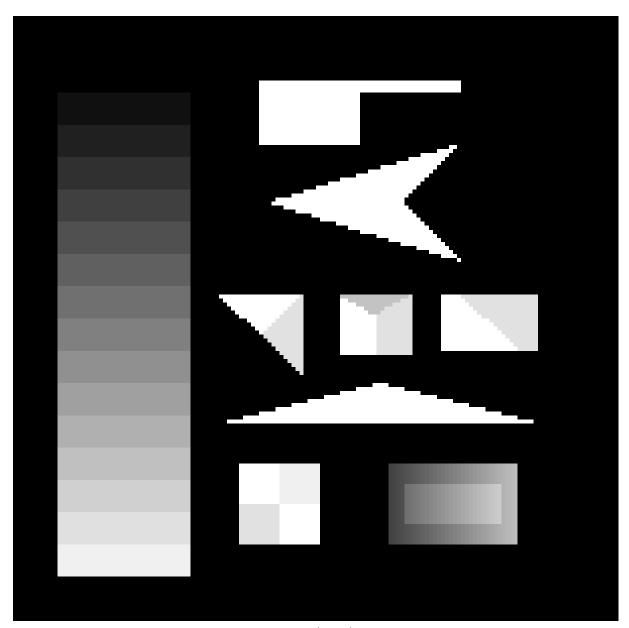
## 4.1 Image Edge Detection

Figure 6 presents a series of snapshots from an optimal edge detection experiment. The given image here is a  $150 \times 150$  256-gray-level digital image. It was used as the grid lattice for a class of autonomous agents. Initially, a group of 100 agents was randomly distributed in the lattice. Since this is a relatively small number of agents, the majority of them will not immediately find the image features, but rather after a few randomized movements as illustrated in Figure 6(t=4). In the snapshots, the clouds of light-grey dots signify the active autonomous agents that are undertaking certain diffusion processes, and the sequences of dark-grey dots are the markers left by the agents once they encounter the feature pixel locations.

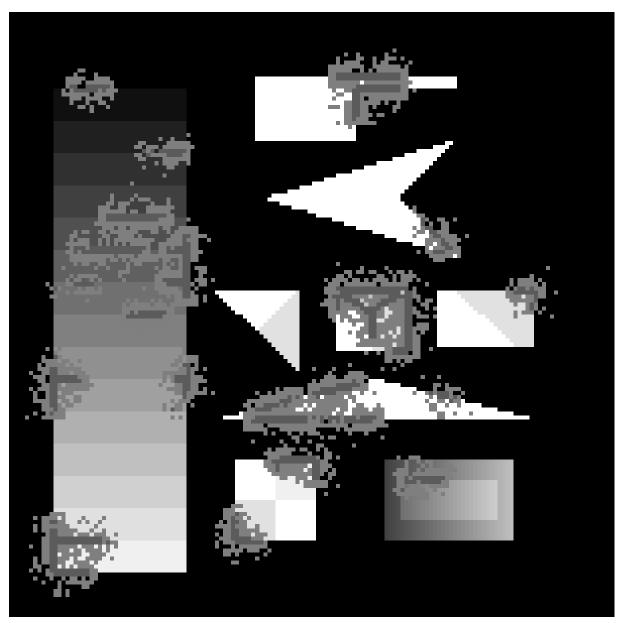
By definition, the number of total diffusion movements allowed is determined by the life span of the agents. In this experiment, the life span of the agents was set to 3. Therefore, if an agent does not find any features during the interaction with its environment for more than three discrete time steps, it will vanish from the lattice environment. On the other hand, the agents in the environment will asexually self-reproduce offspring agents if the triggering condition of certain density-distribution satisfies a given  $\lambda$  interval. In the present experiment, we set:  $\lambda = [2, 7]$  for a neighboring region of radius  $\kappa = 1$ , the contrast level difference between the current pixel (at which an agent resides) and its eight neighboring pixels  $\delta = 42$ , and the number of offspring agents reproduced at a feature pixel s = 5. That is to say, an agent will leave a marker if the density distribution of its immediate neighboring pixels, whose gray-level

```
input: A digital image of size U \times V, in which each pixel has a gray-level value
output: Immobile agents (or markers) over feature pixels
  randomly distribute an initial set of agents, \{\phi_i^{(0)}\}, over the image
  assign the initial agent set to the active agent set: \Phi \leftarrow \{\phi_i^{(0)}\}\
   while \Phi \neq \emptyset do
     for all current \phi \in \Phi do
        if there exists grandparent(s) \phi' of \phi then
        compute the fitness values for all \phi'
           select \phi', s.t. F(\phi') > 0
           update P(\Theta)_{\phi} and P(\Omega)_{\phi}, using Eqs. 4 and 5, respectively
        else
           assign P(\Theta)_{\phi} and P(\Omega)_{\phi} to uniform distributions
        endif
        if at local triggering stimulus then
           reproduce offspring \{\phi^{(g+1)}\}\ in direction \omega \in \Omega with P(\Omega) to a neighboring sector of radius \kappa
           \Phi \leftarrow \Phi \cup \{\phi^{(g+1)}\}
           become immobilized (or leave a marker) at the current location
           \Phi \leftarrow \Phi - \phi
        else
           if age = life_span then
              \Phi \leftarrow \Phi - \phi
              remove agent from the image
           else
              diffuse to a neighboring sector of radius \kappa, in direction \theta \in \Theta with P(\Theta)
              age_{\phi} \leftarrow age_{\phi} + 1
           endif
        endif
     endfor
   endwhlie
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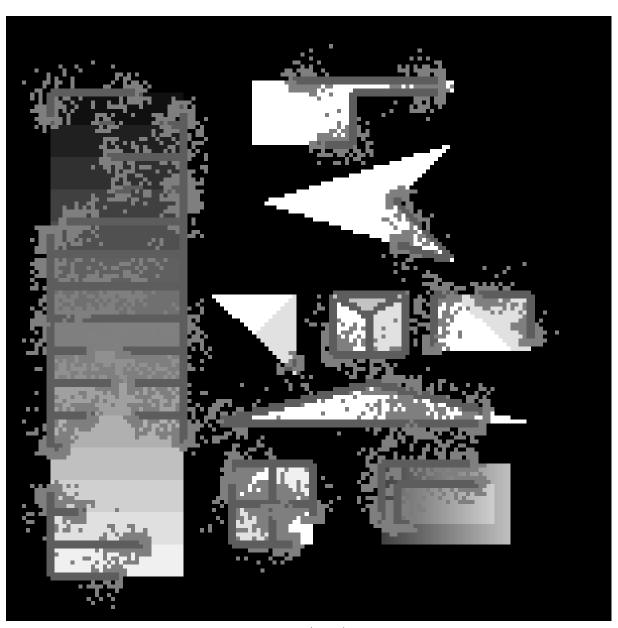
Figure 5: The agent behavioral control and computation algorithm.



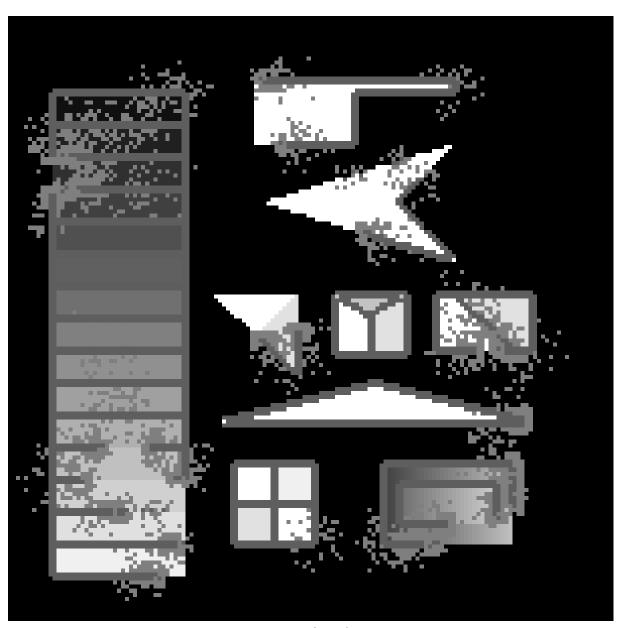
t = 0 (Fig.6)



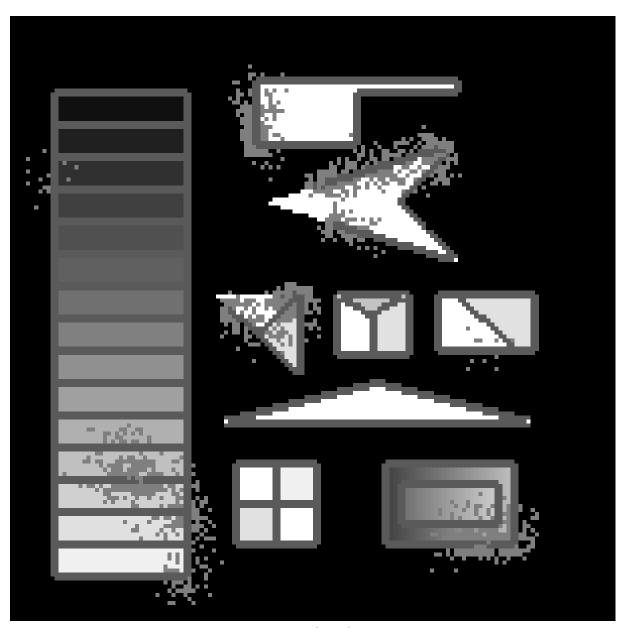
t = 4 (Fig.6)



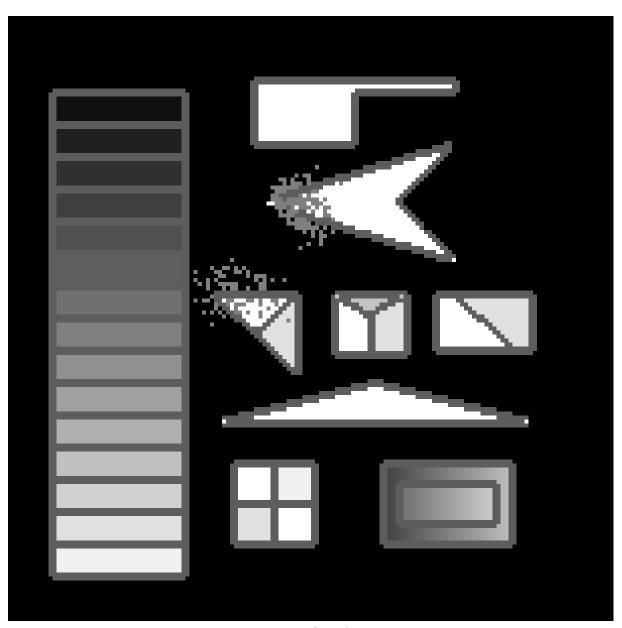
t = 8 (Fig.6)



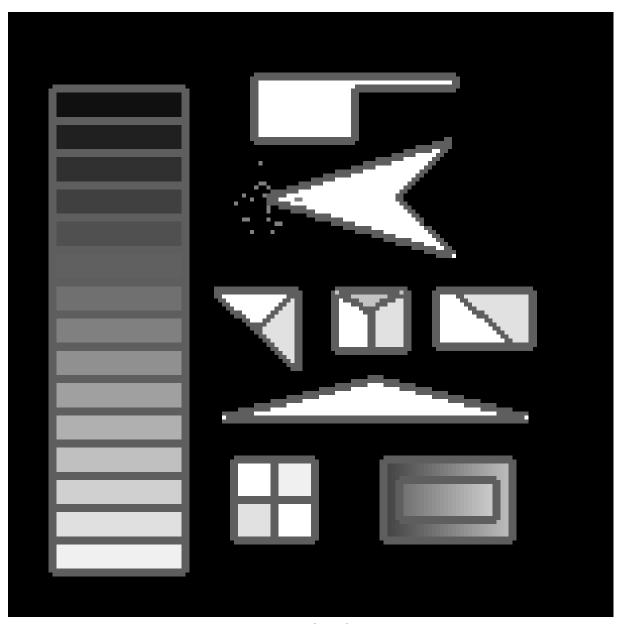
 $t = 12 \; (\text{Fig.6})$ 



t = 16 (Fig.6)



 $t = 20 \; (\text{Fig.6})$ 



t = 24 (Fig.6)

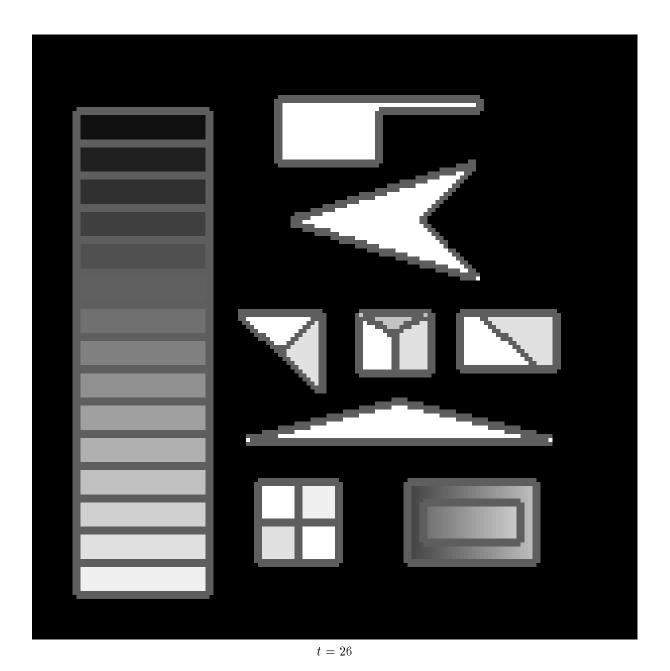


Figure 6: The extraction of edges from a digital image based on the proposed autonomous agent-based computation model. Note that the triggering condition for the behaviors of an agent is computed from the eight-connected neighbors of the agent. The original input image is the one as labeled t=0. The following images show the evolution of the agent population over the two-dimensional lattice. At t=26, all image features (i.e., region borders in this case) are found and labeled with markers.

intensity values are not deviated from that of the current location by 42, falls into the specific interval of [2, 7].

# 4.1.1 Effects of Individual Behaviors on Feature Extraction

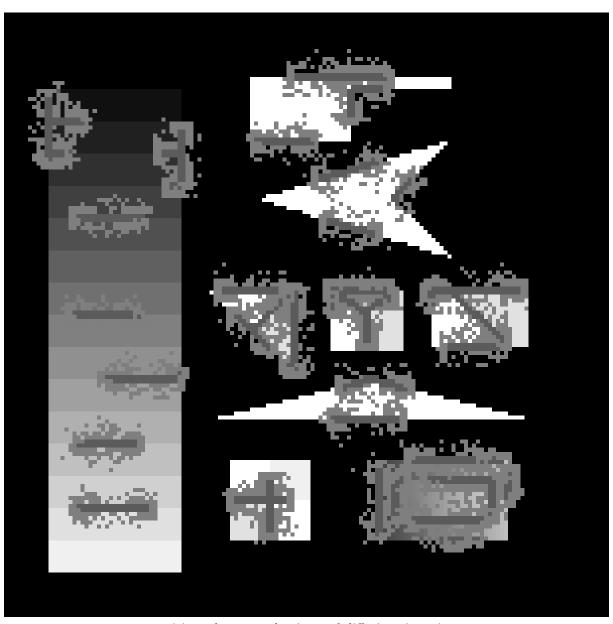
In order to examine the effects of individual behaviors on the efficiency of optimal image feature extraction, we further conducted three experiments that corresponded to the following three conditions, respectively:

- Mode 1. Random Reproduction and Diffusion: The directions for the agent to self-reproduce and diffuse within a neighboring region of radius  $\kappa = 2$  (i.e., the evenly divided sectors within a  $5 \times 5$  region for self-reproduction and diffusion) are randomly determined;
- Mode 2. Directional Diffusion: The direction for the agent to self-reproduce is randomly determined whereas the direction for diffusion is determined according to an updated direction vector; and
- Mode 3. Directional Reproduction: The directions for self-reproduction and diffusion are determined according to updated direction vectors.

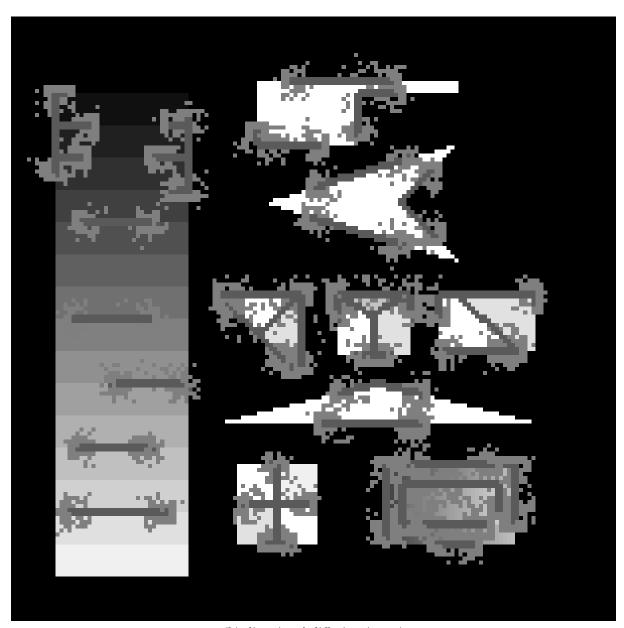
Figure 7 presents three snapshots of the agent evolution under the above mentioned experimental conditions where the age of the agents was set to 3, the number of offspring agents reproduced was set to 8, and  $\lambda = [2, 7]$ . From the figure, it can be observed that the shapes of the active agent clouds were different among the three conditions. In particular, Mode 1 produced the largest clouds evenly distributed along the detected feature pixels. While the active agents in both Modes 2 and 3 progressed effectively along the local feature pixels, the layers in the latter case were relative thinner. This is due to the fact that the maximum size of the self-reproduction or diffusion region in both cases was set to  $5 \times 5$ . Hence, as only one directional sector was selected in the latter case, the actual reproduction sector became limited to the size of four pixels (i.e., only four out of eight reproduced agents were actually kept).

In addition to these observations, several quantitative comparisons were also conducted, the results of which have been shown in Figures 8 to 10. Figure 8 gives the number of active agents as involved in the region border extraction. Modes 1 and 2 were similar in agent population size, the former used slightly more than the latter. Mode 3 used a smallest number of agents during the initial half of the evolution period, and had slightly more agents later for a short period. Figure 9 shows a comparison of the accumulated feature pixels as detected in the three modes. Mode 2 was slightly faster than the random mode, while Mode 3 was slightly slower since fewer agents were reproduced each time for reasons as mentioned in the preceding paragraph.

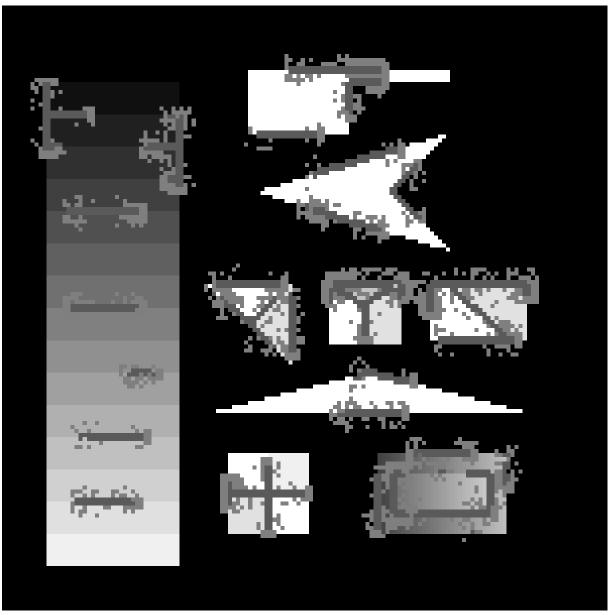
Of greatest interest is Figure 10 which compares the efficiency measures among the three modes. From this figure, Mode 3 represents by far the most efficient means for optimal feature extraction as its averaged measure is consistently higher than Modes 1 and 2.



(a) random reproduction and diffusion (Fig.7)



(b) directional diffusion (Fig.7)



(c) directional reproduction

Figure 7: The snapshots of agent evolution under three different experimental conditions (see text).

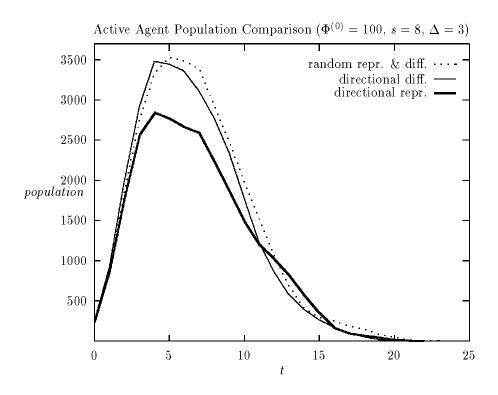


Figure 8: A comparison of active agents in the two-dimensional lattice over the entire period of evolution.

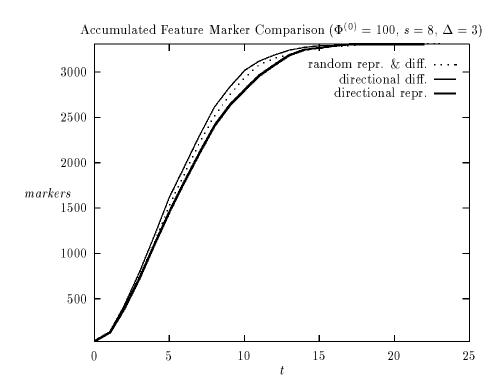


Figure 9: A comparison of accumulated feature pixels as detected over the entire period of evolution.

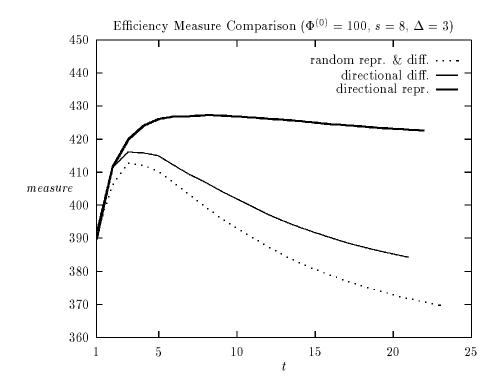


Figure 10: A comparison of the efficiency measures in optimal feature extraction.

#### 4.1.2 Parameters Affecting Agent Computation

With respect to the experiment as presented in the preceding subsection (for Mode 1), we further investigated the effect of initial population size on the dynamics of the evolution, and found that the total number of active agents involved was not affected by the number of initial agents. However, the rates of self-reproduction and death can be affected.

In Figure 11(a), the dynamics of autonomous agent populations with different initial sizes (i.e., 200, 400, and 800) and 5-step life span is presented. The areas under the three curves are almost the same, and the curve under higher initial population size converges faster.

Apart from the initial population size, the second factor that is of interest is the life span of the agents. Our experiments showed that if the life span increased, diffusion toward other features would become more likely to occur. This phenomenon can be observed from Figure 11(b), i.e., the slight differences among the population curves of active agents with three different life span values, respectively.

## 4.2 Character Border Searching

Figures 12(a)—(i) present the evolution of agents in a digital image. The final result of agent evolution, as shown in Figure 12(i), gives the external borders of two characters. In the experiment, the initial population size was set to 40. The neighboring region, from which the triggering condition was verified, was composed of two consecutive layers from the current location of the agent. Or, in other words, the radius of the triggering region,  $\kappa$ , was equal to 2. The  $\lambda$  interval was set to [1-10] for the triggering condition. Furthermore, the threshold for the gray-level contrast,  $\delta$ , was set to 0. Other parameters such as life span were exactly the same as those in the previous experiment.

#### 4.3 Multiple Feature Extraction

All the experiments mentioned so far were concerned only with single-class agents that effectively search and mark their feature pixels. In order to demonstrate the effects of multiple classes of agents in the simultaneous extraction of significant image features, we have conducted an experiment in which three different classes of agents were designed to extract features from a more complex image as shown in Figure 13(a). The specifications of the three classes are as follows:

```
Class 1: \delta = 50, \lambda = [0, 11], \Phi^{(0)} = 350, s = 8, and \Delta = 5;
```

**Class 2**: 
$$\delta = 50$$
,  $\lambda = [10, 20]$ ,  $\Phi^{(0)} = 350$ ,  $s = 8$ , and  $\Delta = 5$ ; and

Class 3 : 
$$\delta = 50$$
,  $\lambda = [20, 23]$ ,  $\Phi^{(0)} = 210$ ,  $s = 8$ , and  $\Delta = 5$ .

Initially all three classes of agents were randomly distributed over the two-dimensional lattice which corresponds to the horizontal grids of the plot in Figure 13(b). Note that the vertical dimension as defined over the lattice shows the intensity values of the grid pixels. In searching for different image features, the agents of different classes would check and react to their local pixels in a manner as defined in Section 3.3. After a number of behavioral evolution steps, the populations of active agents belonging

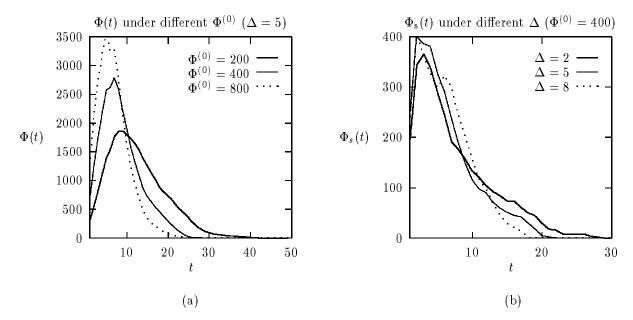
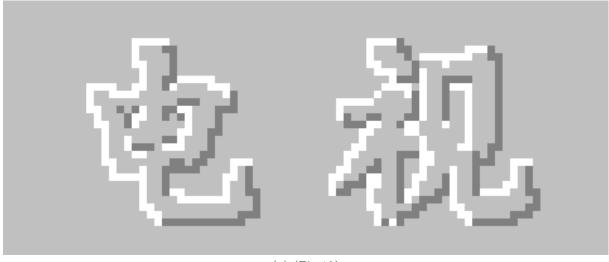
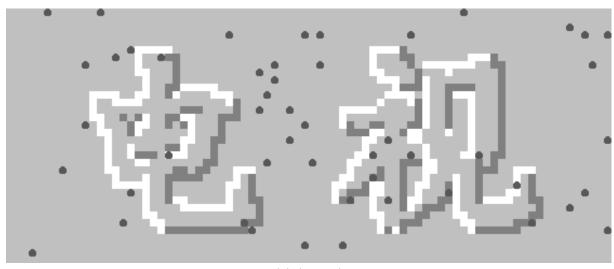


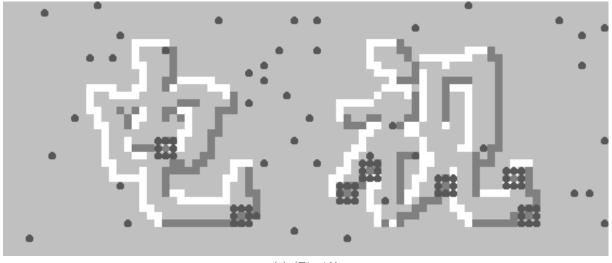
Figure 11: (a) The dynamics of agent population in the case of edge-detection experiment, under three different initial population sizes, where  $\Phi(t)$  curve shows the total number of active agents existing in the lattice. (b) The effect of different life span values on the dynamics of feature extraction, where  $\Phi_s(t)$  curve shows the total number of active agents that have found image features during their interaction with the environment.



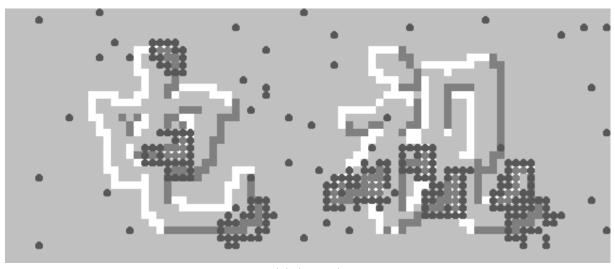
(a) (Fig.12)



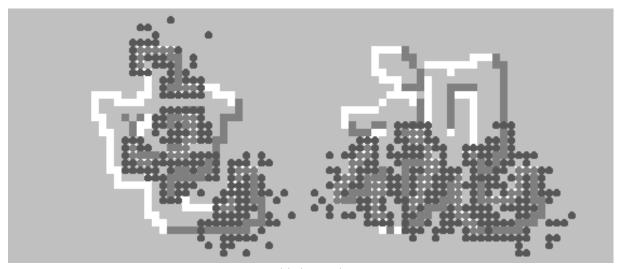
(b) (Fig.12)



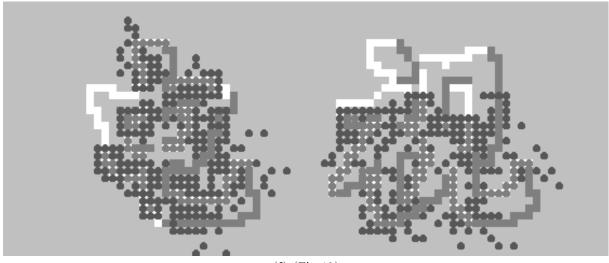
(c) (Fig.12)



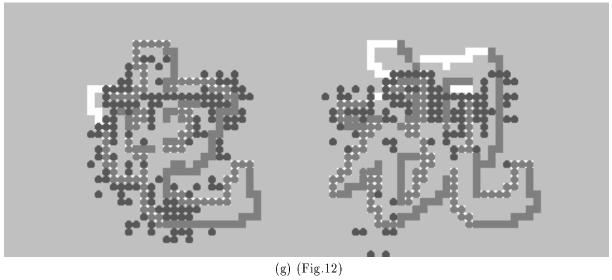
(d) (Fig.12)

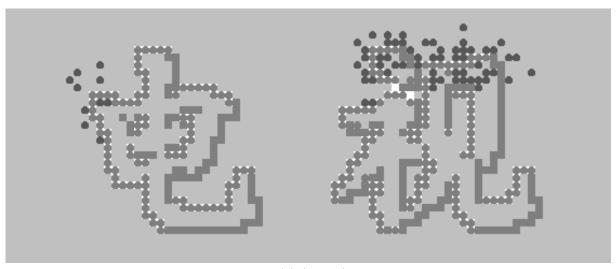


(e) (Fig.12)



(f) (Fig.12)





(h) (Fig.12)

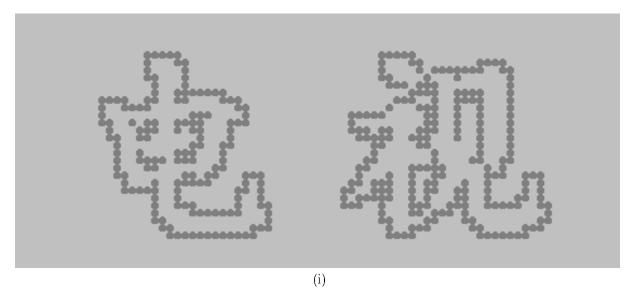
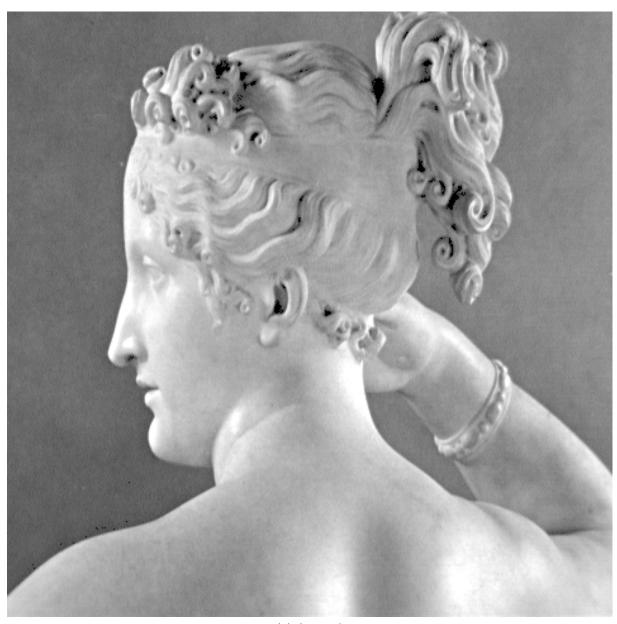
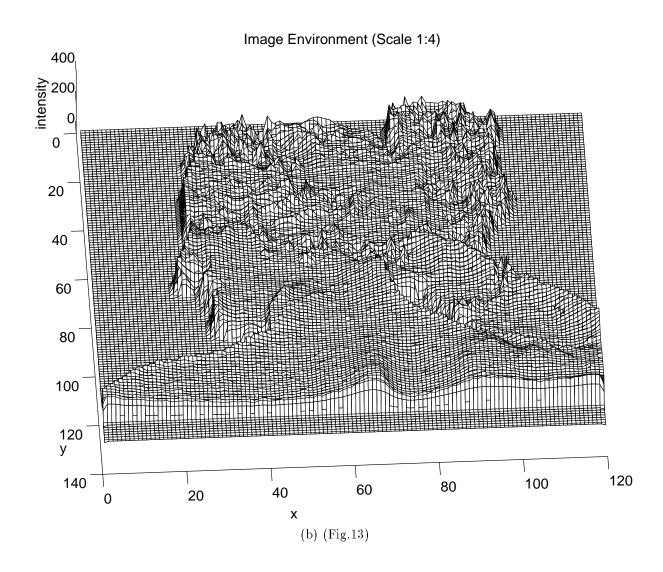
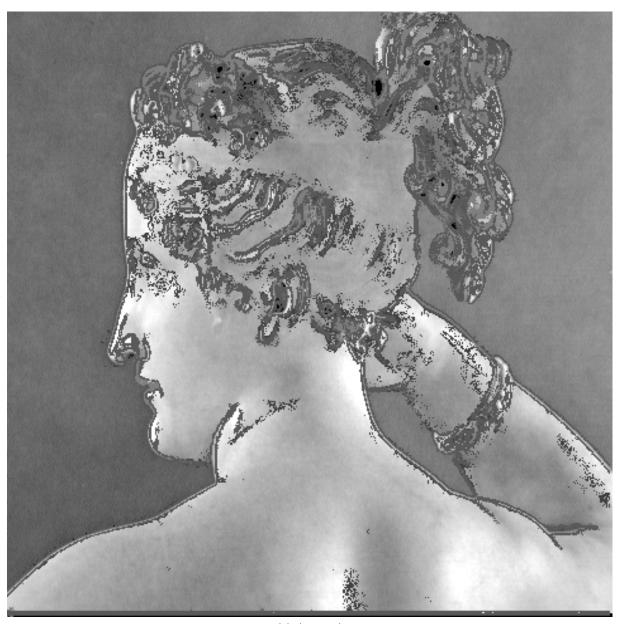


Figure 12: An example of autonomous agents for extracting borders of two characters. (a) shows the original image, (b)-(h) provide the snapshots of the intermediate steps in border extraction, and (i) shows the feature-markers, representing the found borders. It can be noted that the agents are sensitive to those locations that satisfy the triggering condition, i.e.,  $\lambda = [1, 10]$  and  $\kappa = 2$ .



(a) (Fig.13)





(c) (Fig.13)



(d) (Fig.13)



(e) (Fig.13)

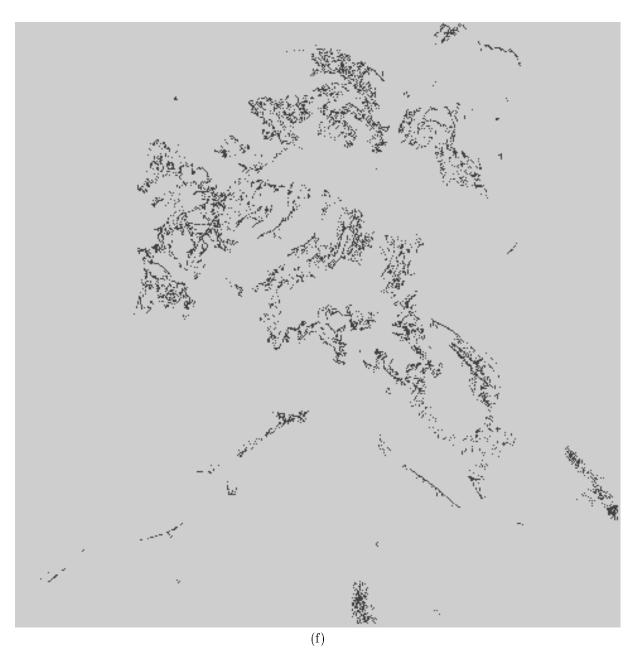


Figure 13: The extraction of face features using three different classes of autonomous agents. (a) The original image is in 256 gray-level intensity of size  $520 \times 480$ . (b) The gray-level image is shown in a three-dimensional plot (scale = 1:4) in which the vertical axis represents the intensity levels of pixels. The horizontal dimensions of the plot represent the size of the two-dimensional lattice in which the autonomous agents reside and evolve. (c) After a period of discrete time, the three classes of the agents completely marked their "territories", i.e., corresponding image features. (d) The features as marked by Class 1 agents correspond to the sharp-contrast region pixels. (e) The features as marked by Class 2 agents correspond to the significant narrow edges. (f) The features as marked by Class 3 agents correspond to the mild sloping surface regions.

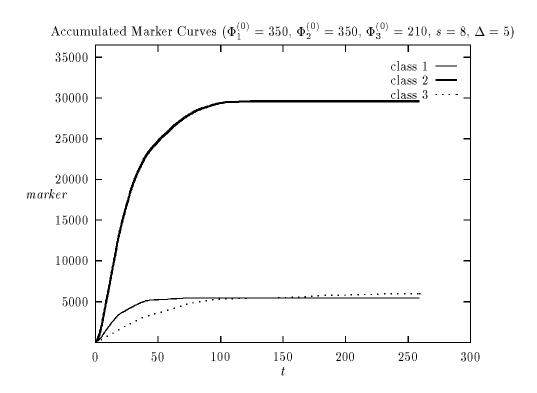


Figure 14: Accumulated marker curves. The three classes of agents effectively find all their corresponding feature pixels after 100 steps.

to the three classes would gradually vanish as all the features became emerged. The final results of feature-markers as left by the agents are shown in Figure 13(c).

In order to get a clear view of the features, Figure 13(c) is further decomposed into three separate figures, one for each type of features as detected by a particular class of agents. More specifically, Figure 13(d) shows the highest contrast region pixels as found by Class 1 in the hair, ear, and mouth regions. These feature regions identify the most significant corner sketches of the image. Figure 13(e) shows the result of Class 2 in extracting all the narrowly connected edge pixels. The edge markers give a meaningful outline of the image. Finally, Figure 13(f) presents the features as marked by Class 3, which correspond to the mild sloping surface regions, i.e., shadows that reflect the overall shape/depth information of the image.

The rate of feature extraction varies from one class to another. Figure 14 gives the accumulated marker curves for all the three classes. It is noted that Class 2 has the highest extraction rate, whereas Class 3 has the lowest. This is mainly due to the fact that the designed agent behaviors, such as diffusion and self-reproduction, are more effective in searching and branching the high-connectivity features.

## 4.4 Image Feature Tracking

The previous sections have provided the details on the local mechanism and the global dynamics of agents in *static* digital image environments, and shown how the features can be searched as a result of behavioral evolution. As a step further from the static image environments, this section examines the capability of autonomous agents in following detected features in a sequence of digital image frames. This task represents one of the most challenging image-processing problems, namely, visual tracking and motion estimation for robot vision [6, 7].

Figure 15 shows an overlaid view of multiple digital image frames, each of which gives the location of an object at a certain discrete time. The problem of image feature following in this case can be stated as follows: Suppose that at a specific time, the image features have been identified in a manner as in the static-environment case. However slightly unlike the previous experiments in which the agents marked the feature pixels whenever their search succeeded, this experiment will disable the feature-marking behavior but instead permit the active agents to reside (i.e., become immobilized) at the feature pixels. After some intervals of time, the image features move to new locations, and subsequently, some of the previously successful agents will no longer be at the feature locations, as illustrated in Figure 16. When such an instance occurs, the agents that previously immobilized at the feature pixels will be activated again as if they were just reproduced. They will adjust their diffusion and self-reproduction directions in order to maximize their fitness in the new environment (i.e., local fitness optimization). This in turn enables the agents to relocate the features. Figure 17 presents the experimental results concerning the adaptation of the agents in the dynamic environment in which a T-shaped object moves in time, as shown in Figure 15. The learning curve in Figure 17 indicates the time as required for the population of the agents to adapt to a new feature movement.

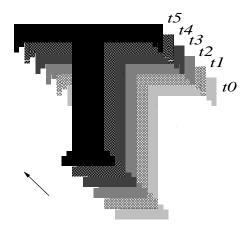


Figure 15: An example dynamic environment in which a T-shaped object moves in discrete space and time.

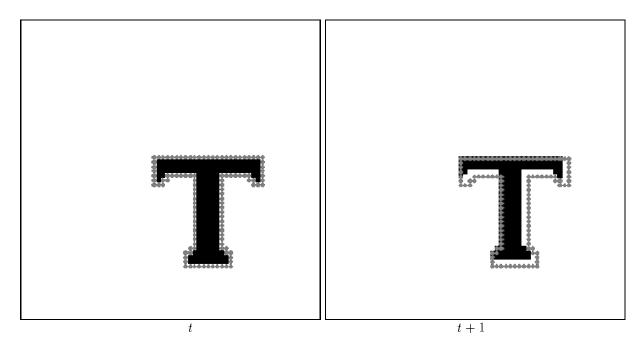


Figure 16: (a) At time t, agents have located the border of a T-shaped object from the environment. (b) At time t + 1, the T-shaped object moves to a new location, resulting in previously successful agents to be offset from the feature pixels.

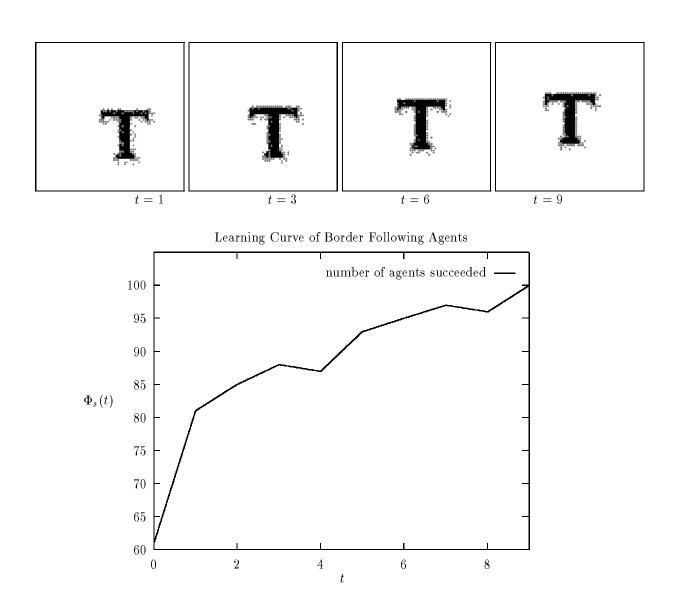


Figure 17: The snapshots of the feature following agents and their learning curve. After the target has been moved, some of the agents will attempt to move towards the target based on the evolved behaviors. Agents that have found the edge will diffuse locally and then become immobilized, and the ones that did not find the edge grid during their life span will vanish from the two-dimensional lattice.

## 5 Discussions

This section gives some further observations on the proposed evolutionary autonomous agents, concerning their population dynamics and relationships to adaptation.

# 5.1 The Dynamics of Evolutionary Autonomous Agents

In order to enable a better understanding of the empirically obtained results on agent population change as shown earlier, what follows provides a formal description of the agent dynamics.

At a discrete time k, the number of agents that succeed in locating the features can be calculated as follows:

$$R_k = \sum_{i=1}^{\Delta} \psi_k^{k-i} \tag{7}$$

where  $\Delta$  denotes the life\_span of the agents, and  $\psi_k^{k-i}$  denotes all the agents that were reproduced at time k-i and found the features at time k.

Based on the above definition, we can further derive the equation for computing the agents that vanish at time k, as follows:

$$W_k = \alpha R_{k-\Delta} - \sum_{i=k-\Delta+1}^k \psi_i^{k-\Delta}$$
 (8)

where  $R_{k-\Delta}$  is computed using Eq. 7, and  $\alpha$  denotes the number of offspring generated as exually by a single self-reproducing agent. The first term of this equation indicates all the agents reproduced at time  $k-\Delta$ . The second term indicates how many of them have found the feature pixels during a period from time  $k-\Delta$  till time k. In other words, this equation expresses that the agents will vanish at time k if they exceed their life span.

Eqs. 7 and 8 determine the entire population of active agents at time k. The equation reads:

$$U_k = U_0 + \sum_{j=1}^k (\alpha R_j) - \sum_{j=\Delta}^k W_j$$
 (9)

where  $U_0$  denotes the number agents initially distributed over the two-dimensional lattice.

Substituting  $R_j$  and  $W_j$  with Eqs. 7 and 8, respectively, yields:

$$U_k = U_0 + \alpha \sum_{j=1}^k \sum_{n=1}^{\Delta} \psi_j^{j-n} - \sum_{j=\Delta}^k (\alpha \sum_{n=1}^{\Delta} \psi_{j-\Delta}^{j-\Delta-n} - \sum_{n=j-\Delta+1}^j \psi_n^{j-\Delta}).$$
 (10)

It can readily be noted that the growth rate of the active agent population is *positive* if the following is satisfied:

$$\alpha R_k - W_k > 0. \tag{11}$$

Based on Eqs. 7 and 8, we can rewrite the above condition as follows:

$$\alpha R_k > \alpha R_{k-\Delta} - \sum_{i=k-\Delta+1}^k \psi_i^{k-\Delta}. \tag{12}$$

What may also be inferred from the above is that the growth rate of agents will decrease after the markers curve and the agent death curve intersect. The growth rate switches from positive to negative when the

death rate is the highest.

## 5.2 A Continuous Model of Evolutionary Autonomous Agent Dynamics

The dynamics curves of the agent population as presented in Figure 11 have offered the behavioral description of a dynamic population system that diffuses in discrete time with a time delay distributed over a specific interval of time. As a matter of fact, the shape of the population distribution as obtained from our experiment fits very well with that of the following continuous integro-differential equation as often used to model a logistic growth with distributed time delay [2], which reads:

$$\frac{1}{N(t)}\frac{dN(t)}{dt} = a - b \int_{-\infty}^{t} K(t-z)N(z)dz. \tag{13}$$

If let U = Nb/a, T = at, M = bP,  $\sigma = s/a$ , and  $\Gamma = r/a$ , a special case solution can be written as follows:

$$U = U_0 exp \left[ (1 - \rho)T + \frac{\rho}{\sigma} (1 - e^{-\sigma T}) \right]$$

$$\tag{14}$$

where  $\rho = \Gamma U_0 / \sigma$ .

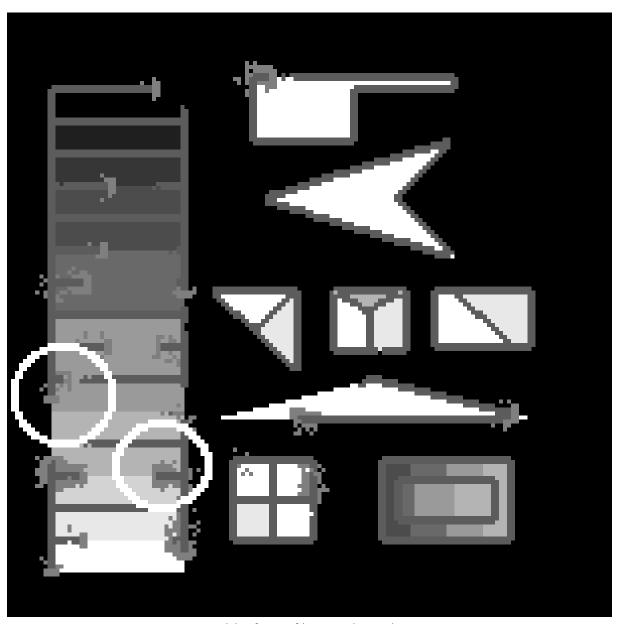
The derivation of Eq. 14 can be found in [2]. Some of the mathematical background readings on nonlinear partial differential equations can be found in [27].

#### 5.3 Balance between Evolution and Adaptation

In our experimentation, we have noted that there are some cases in which the inherited diffusion and self-reproduction directions could slow down the agents in adapting to their new local stimulus. Figure 18(a) identifies two spots where this phenomenon is observed: one inside the upper-left circle and the other inside the lower-right circle. As shown in Figures 18(b)-(e), in the former case the agents failed to branch horizontally to the new feature pixels, whereas in the latter the agents gradually stopped progressing along the preceding feature pixels.

Both cases occurred when the life span (or maximum age) of the agents was set shorter than 3. In other words, the agents would have a great inertia to move or self-reproduce in the directions as inherited from the previously selected parent agents. Even though some of the offspring agents encountered new stimuli from other directions, the inherited directions had a strong bias that dominated the agent behaviors. This problem can be remedied if we allow the agents to survive for a longer period of time or we introduce a certain random movement and self-reproduction in the sectors other than the one as updated from the parent agents. In both cases, the agents would have a chance to gradually alter the preceding course of evolution.

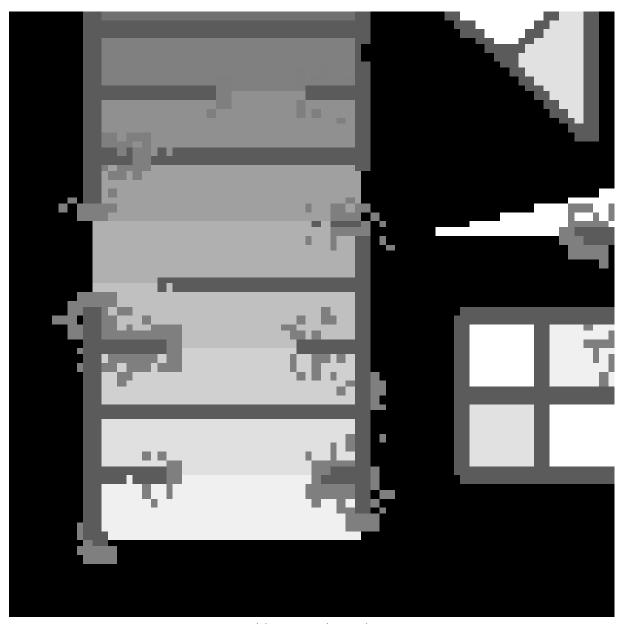
The above observation has raised an interesting issue on the balance between the influence from the selected parent agents and the degree of freedom for the current agent to adapt. Our experiments have shown that it is always necessary to avoid the two extreme cases of agent behavioral selection, i.e., (1) completely random diffusion and self-reproduction, and (2) complete inheritance.



(a) focus of interest (Fig.18)



(b) t = 27 (Fig.18)



(c) t = 28 (Fig.18)



(d) t = 29 (Fig.18)



Figure 18: (a) Two spots are of particular interest, as identified with circles. (b)—(e) give the intermediate steps of agent evolution within the focused regions. It can be noted that the agents at these two spots have failed to branch (upper-left circle) and progress (lower-right circle) to connected feature pixels.

## 6 Conclusion

This paper described an evolutionary autonomous agent-based approach to image feature extraction. While giving the agent computation algorithm, the paper also presented several experimental results to demonstrate how the evolution of the distributed autonomous agents enables the optimal extraction of image features, and discussed the effects of behavioral parameters on the performance.

The advantages of the proposed approach can be summarized as follows:

- 1. the image feature extraction process is entirely determined by the locality and parallelism of the individual agents; and
- 2. the directions for the diffusion and self-reproduction of the agents are dynamically selected and evolved.

With respect to real-life applications, the proposed approach could have significant impact on difficult image analysis problems, i.e., problems in which conventional edge and contrast enhancement have failed to extract important features. Examples of such applications are:

- identification of pathological foci of early stage cancer and important anatomical features (either not visible or not distinguishable) from ultrasound images of a prostate [30]; and
- identification of spiculated lesions, microcalcifications, and circumscribed lesions in scanning mammograms for breast cancer [14].

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